A projection system includes a projection apparatus embodied in a housing secured to a user. The projection apparatus has a processor in data communication with a networking device, at least one input/output device, and computer memory. The computer memory includes a program with machine readable instructions that, when executed by processor, perform the following steps: (a) determine an edge of a surface to be measured; (b) project an initial image onto the surface, the initial image being based on a predetermined set of conditions; (c) determine a substantially perpendicular distance D1 between the projection apparatus and the surface; (d) determine a distance D2 between the projection apparatus and the edge of the surface; (e) calibrate the initial image based on the distances D1 and D2 determined in steps (c) and (d); and (f) project an updated image onto the surface.
600 USER DETERMINES SURFACE 100 TO BE MEASURED

602 USER ACTIVATES THE REFERENCE DEVICE 270 AND PLACES IT NEXT TO SURFACE 100

604 USER ACTIVATES PROJECTION APPARATUS 200

606 APPARATUS PROJECTS INITIAL IMAGE 150 ONTO SURFACE 100

608 USER SELECTS DESIRED IMAGE FROM IMAGE DATABASE 223 AND DESIRED IMAGE IS STORED IN MEMORY 220

610 PROCESSOR 205 ACTIVATES OUTPUT DEVICE 215 TO MEASURE DISTANCE L1

610a PROJECTOR APPARATUS 200 COMMUNICATES WITH REFERENCE DEVICE 270 TO DETERMINE DISTANCE L2

610b PROCESSOR 205 DETERMINES LENGTH L3 AND ANGLE θ

610c PROCESSOR 205 DETERMINES A FACTOR TO ALTER PROJECTED IMAGE 150 AND ALTERS IMAGE ACCORDINGLY

610d PROCESSOR 205 PROJECTS ALTERED IMAGE ONTO SURFACE

612 USER LOCKS IMAGE

614 USER UNLOCKS IMAGE

616 USER DEACTIVATES PROJECTION APPARATUS 200

FIG. 6
PROJECTION MAPPING SYSTEM AND APPARATUS

FIELD OF INVENTION

The invention relates to projection mapping apparatus. More specifically, the invention relates to an apparatus for projecting a tape measure onto a surface.

BACKGROUND

Projection displays have been around for several years in many different forms. While many industries take advantage of projection technology, one industry where such technology has been largely ignored is hand tools. Generally speaking, hand tools have seen relatively few advancements over the years. This is especially true when it comes to tape measures.

Currently, tape measures are effective for their intended purpose. However, they tend to be bulky and somewhat difficult to use, as a user must both lay out the tape measure upon a surface and mark the surface while attempting to hold the tape measure in position. This often results in frustration, especially when the tape measure becomes dislodged from its desired position, twists, or the user has to take measure many different surfaces. Accordingly, it would be desirable to have a projection tape measure which allows a user to measure a surface without requiring him or her to physically hold any device.

SUMMARY

The following presents a simplified summary of the invention in order to provide a basic understanding of some aspects of the invention. This summary is not an extensive overview of the invention. It is not intended to identify critical elements of the invention or to delineate the scope of the invention. Its sole purpose is to present some concepts of the invention in a simplified form as a prelude to the more detailed description that is presented elsewhere herein.

In one embodiment, a projection system includes a projection apparatus embodied in a housing secured to a user. The projection apparatus has a processor in data communication with a networking device, at least one input/output device, and computer memory. The computer memory includes a program having machine readable instructions that, when executed by processor, performs the following steps: (a) projecting an initial image onto the surface, the initial image being based on a predetermined set of conditions; (b) determining a substantially perpendicular distance D1 between the projection apparatus and the surface; (c) determining a distance D2 between the projection apparatus and the reference device; (d) calibrating the initial image based on the distances D1 and D2 determined in steps (b) and (c); (e) projecting an updated image onto the surface; and (f) repeating steps (b)-(e). The reference device and the projection apparatus communicate over a network.

In still another embodiment, a projection system has a reference device and a projection apparatus embodied in a housing secured to a user. The projection apparatus includes a processor in data communication with a networking device, at least one input/output device, and computer memory. The computer memory includes a program having machine readable instructions that, when executed by processor, perform the following steps: (a) projecting an initial image onto the surface, the initial image being based on a predetermined set of conditions; (b) determining a substantially perpendicular distance D1 between the projection apparatus and the surface; (c) determining a distance D2 between the projection apparatus and the reference device; (d) calibrating the initial image based on the distances D1 and D2 determined in steps (b) and (c); (e) projecting an updated image onto the surface; and (f) repeating steps (b)-(e).

FIG. 1 is a schematic illustration of a projection apparatus and system according to an embodiment of the invention.

FIG. 2A is a front view of an embodiment of the projection apparatus of FIG. 1.

FIG. 2B is a side view of the projection apparatus of FIG. 2A.

FIG. 3 is a perspective view of the projection apparatus of FIG. 2A incorporated into a hat.

FIG. 4A is a side view of another embodiment of the projection apparatus of FIG. 1.

FIG. 4B is a front view of the projection apparatus of FIG. 4A.

FIG. 5 is a perspective view of the projection apparatus of FIG. 4A incorporated onto a pair of glasses.

FIG. 6 is a flowchart illustrating various steps performed by projection apparatus systems according to an embodiment of the invention.

FIG. 7 is a perspective view of a projection apparatus system according to an embodiment of the invention.

FIG. 8 is a perspective view of a projection apparatus system according to still another embodiment of the invention.

FIG. 9 is a perspective view of a projection apparatus system according to yet another embodiment of the invention.

DETAILED DESCRIPTION

Currently, the majority of hand tools do not incorporate any type of projection system. One exception is distance finders which use ultrasonic and/or laser reflection techniques to determine a distance from the user to a surface. The user points the tool at a surface, presses a button to activate the laser, and the tool measures the distance to the location where the laser is pointed. While these devices are useful for determining the distance to a point, they are not
tape measures. A tape measure cannot be substituted for a laser pointer where the user desires to, for example, mark a surface for cutting.

Disclosed herein are embodiments of projection mapping apparatus which may be useful as a tape measure projection device. Those of skill in the art shall understand that while reference is made herein to apparatus that project tape measures, other projection apparatus are contemplated within the scope of the invention and will become apparent from the description provided herein.

In one embodiment, a projection mapping system and apparatus includes a projection apparatus 200 which may be configured to attach to a user's person or incorporated into an article worn by the user as described herein. Electronic components of the projection apparatus 200 are illustrated in FIG. 1. The projection apparatus 200 includes a processor 205 communicatively coupled to a networking device 210, one or more input/output devices 215, and computer memory 220. The processor 205 may be configured through particularly configured hardware, such as an application specific integrated circuit (ASIC), field-programmable gate array (FPGA), etc., and/or through execution of software (e.g., program 225) to perform functions in accordance with the disclosure herein.

Memory 220 represents one or more of volatile memory (e.g., RAM) or non-volatile memory (e.g., ROM, FLASH, magnetic media, optical media, etc.). Although shown within the projection apparatus 200, the memory 220 may be, at least in part, implemented as network storage external to the projection apparatus 200 which may be accessible via the network device 210. The network device 210 may be implemented as one or both of a wired network interface and a wireless network interface (e.g., Wi-Fi, Internet, Bluetooth, etc.), as is known in the art.

The network device 210 may allow the projection apparatus 200 to communicate over a network 250 with a reference device 270. The network 250 may be a wireless network, such as Wi-Fi, Bluetooth, or other wireless (or wired) network.

Program 225 may be stored in a transitory or non-transitory portion of the memory 220. Program 225 includes machine readable instructions that, when executed by the processor 205, perform one or more of the functions of the device 200. In embodiments, the program 225 may include instructions for calculating distances and scales and projecting an image onto a surface (e.g., surface 100) as described in greater detail below with reference to FIG. 6.

An image database 223 may additionally be stored in the memory 220, or alternately may be stored in remote storage accessible over the network 250. The image database 223 may contain various images of tape measures which may be projected onto a surface 100 via the projection apparatus 200 according to the description provided herein. For example, there may be tape measure images that display measurements according to the metric system, and other tape measure images that display measurements according to the imperial system. Additionally, the user may prefer one color over another, and therefore there may be multiple images of tape measures in varying colors. Traditionalists may prefer the projection to show the tape measure in yellow, which others may prefer a different color (e.g., white, blue, green, orange, etc.). Accordingly, various images may be stored in the image database 223 accessible by the processor 205.

The input/output device 215 may include one or more input and/or output devices which may be embodied in a single device or multiple devices. In one embodiment, the input/output device 215 includes at least a projector for projecting an image onto a surface (e.g., surface 100). The input/output device 215 may additionally include a laser and/or a camera. Optionally, the input/output device 215 includes a UV laser for marking purposes, as is described below. In one embodiment, the input/output device 215 may further include a speaker. The input/output device 215 may further include a button 215A and 215A' (FIGS. 2B and 4B), for example, to allow the user to interact with the apparatus 200 and/or the reference device 270, as described herein.

The reference device 270 may have a processor 275 communicatively coupled to an input/output device 280 and a network device 285. The network device 285 may allow the reference device 270 to communicate over the network 250 with the projection apparatus 200. The input/output device 280 may be an emitting device which emits a signal (e.g., the network 250 which may be received by the projection apparatus 200 in order to determine the distance between the reference device 270 and the projection apparatus 200. Alternately, the reference device 270 may be in communication (e.g., wired or wirelessly) with the projection apparatus 200 to communicate a distance from the projection apparatus 200 to the reference device 270.

The projection apparatus 200 may be embodied in a variety of different devices. In one embodiment, the projection apparatus 200 may be incorporated into a handheld device, similar to a laser measuring device or flashlight. In another embodiment, the projection apparatus 200 may be configured as a clip. FIGS. 2A, 2B, 4A, and 4B illustrate exemplary configurations of a clip. In FIG. 2A, the projection apparatus 200 is embodied in a clip having a housing 230 with apertures formed therein through which one or more input/output devices 215 may extend. It shall be understood by those of skill in the art that the input/output device(s) 215 may not extend all the way through the aperture, but the aperture may allow the input/output device(s) 215 to give and/or receive information to/from the system. The housing 230 further includes a button 215A which the user may use to interact with the apparatus 200. An arm 234 may rotateably attach to the housing 230 via a pin 232 (for example), and may be spring-loaded such that the arm 234 is maintained in a closed position unless the user forcibly opens the arm 234 (e.g., in order to attach the apparatus 200 to a wearable article). FIG. 3 shows a hard hat 400 with a projection apparatus 200 attached thereto. The projection apparatus 200 may alternately be attached to other wearable articles, such as a baseball cap or other type of hat, or to an article of clothing, such as to the user's collar.

In FIGS. 4A, 4B, and 5, an apparatus 200' is configured for attachment to safety goggles 450 or glasses. The apparatus 200' includes a housing 230' and a clip 234' which may be configured to engage with the nose bridge of the glasses 450. The clip 234' may be adjustable to ensure that the apparatus 200' is securely attached to the glasses 450. The apparatus 200' includes at least one input/output device 215, and may additionally include a button 215A' as shown in FIGS. 4B and 5.

The projection apparatus 200 may preferably be adjustable such that the input/output device 215 is appropriately oriented. For example, the housing 230 may be adjustably attached to a plate which may be secured to the arm 234 via the pin 232. The position of the housing 230 may therefore be adjusted as necessary. Alternately, in embodiments, the projection apparatus 200 may be incorporated directly into items such as the hard hat or safety goggles.
The electronic components of the apparatus 200 may be battery operated, solar powered, or may receive power by any other means now known or later developed. In one embodiment, the apparatus 200 includes a rechargeable battery which may be recharged using solar power, electrical power, etc.

The features of the various components described herein shall be further understood by way of examples of the projection apparatus 200 in a use configuration. Referring now to FIG. 6, an exemplary set of process steps is illustrated according to an embodiment of the invention. The process begins at step 600, when the user determines that a surface requires a measurement. At step 602, the user may activate the reference device 270 and places the reference device 270 such that it abuts one end of the surface 100, as shown in FIG. 8. Further discussion of the reference device 270 is provided below.

Moving on to step 604, the projection apparatus 200 is activated. The projection apparatus 200 may be activated via, for example, a button 215A on the apparatus 200. The button 215A may cause the apparatus 200 to turn to an “on” mode. Alternately, the apparatus 200 may be equipped with, for example, a gyroscope which may detect movement of the user’s head. When the user shakes his or her head, the apparatus 200 may be activated.

At step 606, upon activation, the apparatus 200 may project an initial image 150 onto the surface 100 (see FIG. 7). The initial image 150 may not yet be the user’s desired depiction of a tape measure. For example, the projection apparatus 200 may be initially programmed to project an image from the image database 223 of a tape measure showing measurements according to the imperial measurement system. However, the user may prefer that the measurements be shown according to the metric system. Additionally, the initial image 150 may be programmed to project the initial image 150 based on pre-set reference conditions. However, the reference conditions may not accurately portray the position of the user in relation to the surface 100, and therefore, the initial image 150 may project inaccurate units of measurement (e.g., one inch as projected in the initial image 150 is not a true representation of one inch).

Nevertheless, the process moves to step 608, wherein the user selects the desired tape measure image from the image database 223. The user may be able to change the image in order to customize the system of measurement (e.g., imperial or metric) by toggling through the images stored on the image database 223 to arrive at the desired image, e.g., via the button 215A or 215A’. Additionally, the user may be able to select an image that is color preferential to the user. Once the user arrives at his or her preferred image, the user’s preferences may be automatically stored in the memory 220 and recalled each time the user activates the projection apparatus 200.

Moving on to step 610, once the user has selected his or her preferred image, the processor 205 begins the process of calibrating the projected image to the user’s position in relation to the surface 200. As noted above, the projection apparatus 200 may be programmed to project an initial image 150 based on pre-set reference conditions at which the projected image portrays units of measurement in accurate one-inch units. For example, referring again to FIG. 7, the reference conditions may assume that a distance D1 from the projection apparatus 200 to the surface 100 is equal to 2 feet, and the distance D2 from the edge of the surface 105 to the center point CPI of the projected image is 6 inches. At these conditions, a reference angle α between the user and the end of the surface 105, calculated using the equation sin(α) = D1/D2, is 26.56 degrees. At these conditions, the projection apparatus 200 may project an image of a tape measure, wherein the increments of measurement are shown at exactly 1 inch. However, it is unlikely that the user will maintain these reference conditions. As the user moves closer to or away from the surface 100, the scale of the image must be altered such that the projected image still accurately displays the units of the tape measure. Accordingly, the position of the user relative to the surface 100 must be determined.

At step 610a, the processor 205 causes the projection apparatus 200 to activate one or more output devices 215 (e.g., a laser) to measure the actual distance I1 (FIG. 8) from the user U (having the projection apparatus 200 attached thereto) to the center point CP at surface 100. Using techniques known to those of skill in the art, the distance I1 may be ascertained.

At step 610b, the projection apparatus 200 communicates with the reference device 270, e.g., over the network 250 via networking devices 210 and 285, respectively, to determine the location of the reference device 270. Knowing the location of the reference device 270, the processor 205 is able to determine the distance I2 between the projection apparatus 200 and the reference device 270.

The reference device 270 may, in one embodiment, be a smart phone equipped with downloadable software (e.g., a smart phone application) that allows it to communicate with the projection apparatus 200. In order to use the smart phone as the reference device 270, the user may access the smart phone application on the phone, which may, among other things, activate the networking device 285 such that the projection apparatus 200 may communicate with the phone. For example, after the distance I2 is determined, a planar verification display pattern may be projected onto the surface intended to be measured. The projected display pattern could show geometric shapes with known ratios such as squares, circles, etc. The projected sequence of predictable patterns may be shown sequentially along the surface in order to verify that the surface is flat (or being measured on a common plane). Adjustments in software can be made to adjust for planar integrity for any skewing of the plane of measurement. In one embodiment, the software may be configured to adjust for contoured surfaces utilizing 3D mapping and marking techniques including stereoscopic viewing of the projected display pattern.

In embodiments, the reference device 270 may be omitted. For example, in one embodiment, the projection apparatus 200 may include a camera (e.g., as an input/output device 215). Using traditional gradient image processing techniques, the processor 205 may be able to ascertain the end 105 of the surface 100, and thus determine the length I2. In still another embodiment, the end 105 of the surface 100 may be marked with a marker (e.g., via a marking device such as a UV laser, etching, red dot marking, or via any other marker currently in use or later developed). The projection apparatus 200 may be configured to recognize the marker in order to ascertain the position of the end 105 of the surface 100, and thus determine the length I2.

Moving on, at step 610c, the processor 205 determines the missing length I3 based on the Pythagorean Theorem for right triangles: $a^2 + b^2 = c^2$. The unit of the length I3 may be determined based on the user’s selection of the system of measurement. For example, if the user selects the imperial system, then the lengths I1, I2, and I3 may be measured and determined in inches and feet. Alternately, if the user selects the metric system, then the lengths I1, I2, and I3 may be measured and determined in centimeters and meters. More
advanced non-linear methods may alternately be used to calculate the measurement of length $l_1$. One such iterative method involves differential calculus which would allow contourd measurements of surfaces that are not residing on a single flat plane.

Having determined the length $l_1$, the processor 205 then calculates the angle $\theta$ between the user and the end of the surface 105. For example, if the user is 2.7' (32.4 inches) from the surface 100 ($l_1$), and the distance $l_1$ is determined to be 40 inches, then the angle $\theta$ between the user and the end of the surface 105 as determined by trigonometric principles is 35.9 degrees. Once the processor 105 determines the length $l_1$, and the angle $\theta$, the process moves to step 610a. The processor 205 is not limited to a single angle $\theta$ measurement in order to provide more precise results in measurement. Multiple calculations may be made in succession in order to provide a desired precision resulting measurement.

At step 610a, the processor 205 determines the factor by which the size of the projected image must be altered such that the units of measurement of the projected image correspond with the length $l_1$ determined at step 610c. In our example, the ratio of the reference angle to the actual angle is 0.74. Therefore, the image must be scaled down in length by a factor of 0.74. Using methods of scaling known to those of skill in the art, the program may be configured to scale the projected image 150 by the appropriate factor.

At step 610c, the projection apparatus 200 projects the altered image onto the surface 100, wherein the altered image is appropriately scaled based on the position of the user to the surface 100 as described above.

In one embodiment, illustrated in FIG. 9, the user may be a distance $l_1$ from the end of the surface 105. Those of skill in the art may recognize that in order for the projected image to be as accurate as possible, it may be desirable for the user to be positioned such that the projection apparatus 200 is substantially perpendicular to the surface 100. Therefore, to measure distances that are farther away from the end of the surface 105 (e.g., distances greater than the beam angle $\gamma$, or the angle of the beam from the projection apparatus 200), the user may have to move into the general vicinity of the final measurement. The distance $L$ may be greater than the beam angle $\gamma$. Here, the distances $l_1$, and $l_2$ may be determined as described above regarding $l_1$ and $l_2$. Using the Pythagorean Theorem, the program 223 may determine the distance $L$. Additionally, as the beam angle $\gamma$ from the projection apparatus is known, and the distance $l_1$, may be determined as described herein, the distance $l_2$ between the center point of the projection beam and the edge of the beam may be determined. For example, using the equation $\gamma^{-\frac{L_1}{L_1}}$ (wherein $\gamma$ is the beam angle), the program may determine distance $l_2$. Since the user may not be standing at the end 105 of the surface 100, and the beam of projection is limited, the image of the tape measure may start at point $U$, the unit of which may be equal to the distance $l_2$ less distance $L_1$. For example, if the user is standing 20 inches from the end of the surface 105, and the beam projects an image 8 inches across, the point $P$ will show the beginning of the tape measure starting at 16 inches.

The process may repeat steps 610a through 610c in a continuous loop to ensure that the projected image of the tape measure is consistently accurate. In one embodiment, multiple differential calculations may be made and accumulated to provide increased precision over the overall measurement results to the user.

Optionally, in one embodiment, the process moves to step 612, where the user may be able to lock the projected image. For example, the user may press the button 215A or 215A' (e.g., two quick presses of the button) to lock the image in place. Alternately, the user may be able to effectuate a movement by his head to lock the image (e.g., moving his head in a quick up-and-down movement). By locking the image in place, the user may cause the process to stall at step 620 until the image is unlocked. The user may unlock the image at step 614 by pressing the button, shaking his head, or other means. Once the image is unlocked, the process may return to step 610 as described above.

The process ends at step 616 with the user deactivating the projection apparatus 200.

Thus has been described systems, methods, and apparatus for projecting an image onto a surface. Many different arrangements of the described invention are possible without departing from the spirit and scope of the present invention. Embodiments of the present invention are described herein with the intent to be illustrative rather than restrictive. Alternative embodiments will become apparent to those skilled in the art that do not depart from its scope. A skilled artisan may develop alternative means of implementing the disclosed improvements without departing from the scope of the present invention.

Further, it will be understood that certain features and subcombinations are of utility and may be employed without reference to other features and subcombinations and are contemplated within the scope of the claims. Not all steps listed in the various figures and description need to be carried out in the specific order described. The description should not be restricted to the specific described embodiments.

The invention claimed is:

1. A projection system, comprising:
   a projection apparatus embodied in a housing, the projection apparatus comprising:
   a processor in data communication with a networking device, at least one input/output device, and computer memory, the computer memory comprising a program having machine readable instructions that, when executed by processor, perform the following steps:
   (a) determining an edge of a surface to be measured;
   (b) projecting an initial image onto the surface, the initial image being based on a predetermined set of conditions;
   (c) determining a substantially perpendicular distance $D_1$ between the projection apparatus and the surface;
   (d) determining a distance $D_2$ between the projection apparatus and the edge of the surface;
   (e) calibrating the initial image based on the distances $D_1$ and $D_2$ determined in steps (c) and (d); and
   (f) projecting an updated image onto the surface.

2. The system of claim 1, further comprising a reference device in communication with the projection apparatus over a network, the reference device being placed at the edge of the surface wherein the projection apparatus receives a signal from the reference device to determine the distance $D_2$.

3. The system of claim 2, wherein the reference device is a smart phone.

4. The system of claim 1, wherein the initial image is selected from a plurality of images stored in an image database in the computer memory.

5. The system of 4, wherein the image is of a tape measure.
6. The system of claim 1, wherein steps (c)-(f) are continuously repeated.

7. The system of claim 1, wherein the at least one input/output device includes a projector for projecting the image.

8. The system of claim 7, wherein the at least one input/output device includes a laser pointer for measuring the distance D1.

9. The system of claim 1, wherein the projection apparatus housing is configured as a clip.

10. The system of claim 2, wherein the clip is configured for attachment to a hat.

11. A projection system, comprising:
    a reference device comprising a processor in data communication with a networking device and at least one input/output device, wherein the reference device is placed at an edge of a surface to be measured; and
    a projection apparatus embodied in a housing secured to a user, the projection apparatus comprising:
    a processor in data communication with a networking device, at least one input/output device, and computer memory, the computer memory comprising a program having machine readable instructions that, when effected by processor, perform the following steps:
    (a) projecting an initial image onto the surface, the initial image being based on a predetermined set of conditions;
    (b) determining a substantially perpendicular distance D1 between the projection apparatus and the surface;
    (c) determining a distance D2 between the projection apparatus and the reference device;
    (d) calibrating the initial image based on the distances D1 and D2 determined in steps (b) and (c);
    (e) projecting an updated image onto the surface; and
    (f) repeating steps (b)-(e); wherein the reference device and the projection apparatus communicate over a network.

12. The system of claim 11, wherein the initial image is an image of a tape measure selected from a plurality of tape measure images stored in the computer memory.

13. The system of claim 12, wherein the at least one input/output device of the projection apparatus includes a projector.

14. The system of claim 11, wherein the projection apparatus housing is configured to attach to a structure worn by the user.

15. The system of claim 14, wherein the structure is a hat.

16. The system of claim 11, wherein the projection apparatus housing is formed into a structure to be worn by the user.

17. The system of claim 11, wherein the structure is one of a hat or glasses.

18. A projection system, comprising:
    a reference device; and
    a projection apparatus embodied in a housing secured to a user, the projection apparatus comprising:
    a processor in data communication with a networking device, at least one input/output device, and computer memory, the computer memory comprising a program having machine readable instructions that, when effected by processor, perform the following steps:
    (a) projecting an initial image onto the surface, the initial image being based on a predetermined set of conditions;
    (b) determining a substantially perpendicular distance D1 between the projection apparatus and the surface;
    (c) determining a distance D2 between the projection apparatus and the reference device;
    (d) calibrating the initial image based on the distances D1 and D2 determined in steps (b) and (c);
    (e) projecting an updated image onto the surface; and
    (f) repeating steps (b)-(e).

19. The system of claim 18, wherein the reference device is a marker, the projection apparatus being configured to recognize the marker in order to determine distance D2.

20. The system of claim 18, wherein step (d) comprises the following steps:
    (d1) determining an angle θ between the projection apparatus and the reference device based on determined distances D1 and D2;
    (d2) determining the ratio of the angle θ to an angle α, the angle α being determined based on the predetermined set of conditions;
    (d3) altering the initial image based on the ratio determined in step d2.

* * * * *